

# Atomic vibrations in glasses: 50 years ago, today, and in future



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**Kernresonanzfluoreszenz von Gammastrahlung in Ir<sup>191</sup>**

## In future

**Mössbauer effect**

**Glass dynamics**

**new view of nuclear resonant scattering**

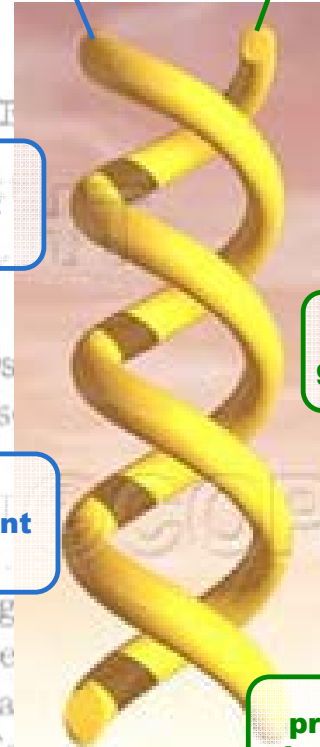
**new view of glass dynamics**

**help from nuclear resonant scattering**

**problems in glass dynamics**

## Today

## 50 years ago



Von  
 RUDOLF L. MÖSSBAUER  
 Mit 3  
 (Eingegangen am 12. Januar 1958)

Die Kernresonanzabsorption der dem Zerfall von Os  
 strahlung in Ir<sup>191</sup> wird untersucht. Der Wirkungs  
 absorption wird als Funktion der Temperatur  
 Temperaturbereich 90° K < T < 370° K  
 Niveaus in Ir<sup>191</sup> ergibt sich zu (3,0  
 zeigt bei tiefen Temperaturen einen starken Anstieg  
 der Absorption für diese Substanzen. Die Theorie  
 absorption langsamer Neutronen in Kristallen wird a  
 von Gammastrahlung übertragen. Bei tiefen Temperat  
 starke Abnahme des Wirkungsquerschnittes für die Kernabsorption von der  
 Frequenzverteilung im Schwingungsspektrum des Festkörpers.

Aus dem Institut für Physik im Max-Planck-Institut für medizinische Physik, Heidelberg

**Mössbauer effect**

**Glass dynamics**

Kernresonanzfluoreszenz von Gammastrahlung in  $\text{Ir}^{191}$

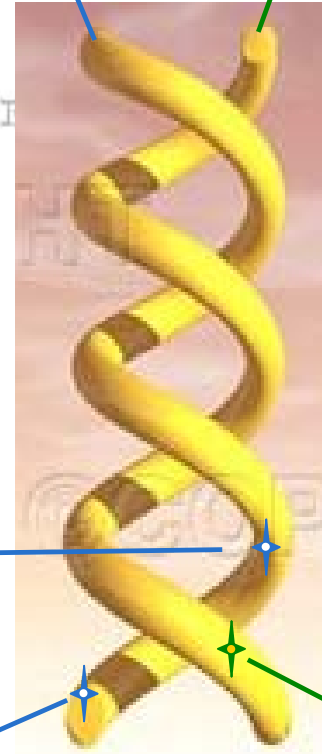
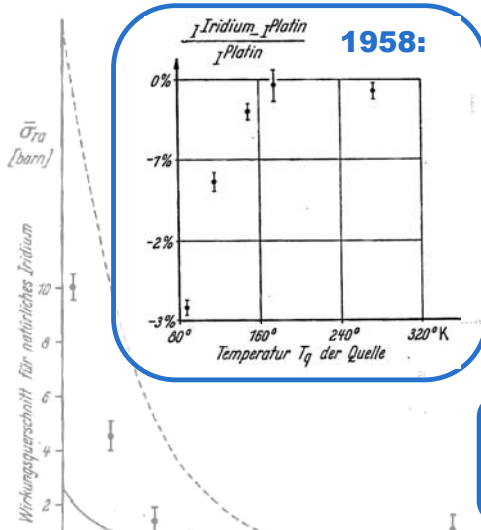
> 50 years

VON  
RUDOLF L. MÖSSBAUER

ago

RUDOLF L. MÖSSBAUER:

jeder vier Intensitäten  $I_i^{\text{Ir}}(T_1)$ ,  $I_i^{\text{Pt}}(T_1)$ ,  $I_i^{\text{Ir}}(T_2)$ ,  $I_i^{\text{Pt}}(T_2)$ . Bei der einzelnen Intensitätsmessung betrug der statistische Fehler 0,04 bis 0,05 % und die Meßzeit 12 bis 20 min. Täglich wurde eine Meßreihe aufgenommen. Um systematische Fehler auszuschließen, wurde die Geometrie bei jeder Meßreihe etwas variiert, durch Drehung der Absorber

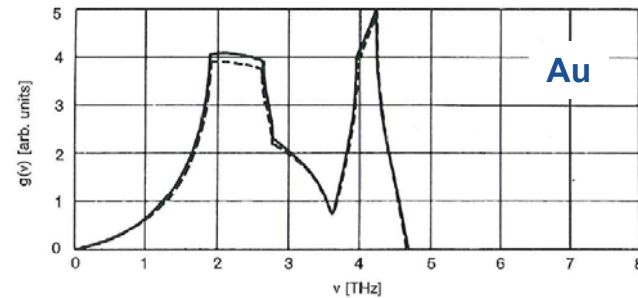
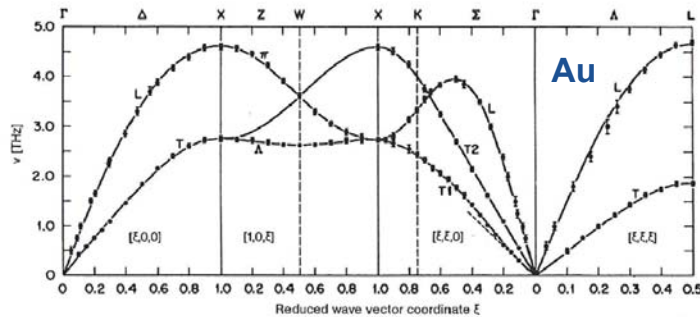
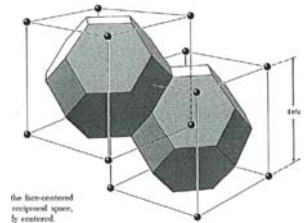
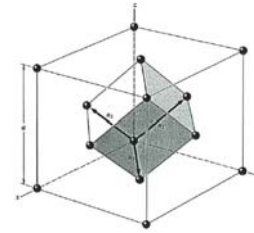
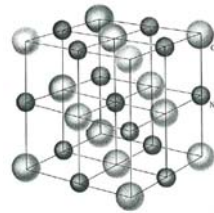


**before 1958:  
nuclear absorption  
increases with  $T^\circ$  ?**

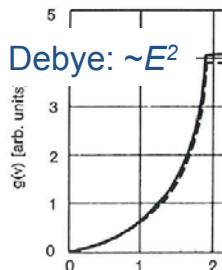
**before 1971:  
glass dynamics:  
sound waves ..?**

## before 1971:

**Crystals: translational periodicity**



**Glasses: no periodicity, no zone boundaries: ideal elastic medium**



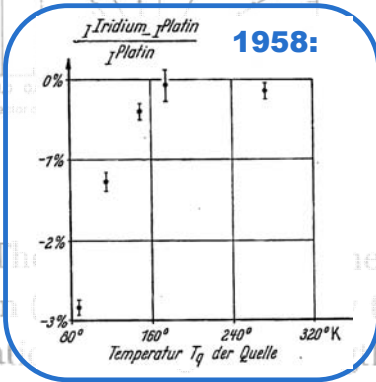
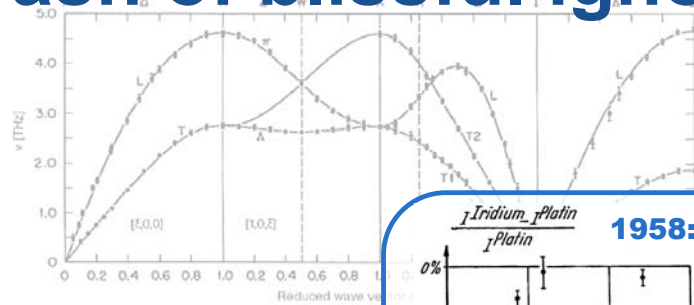
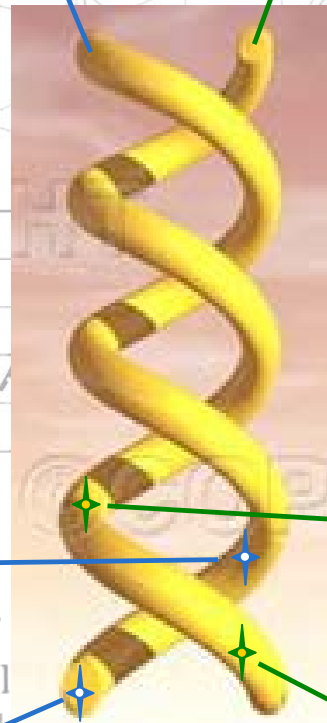
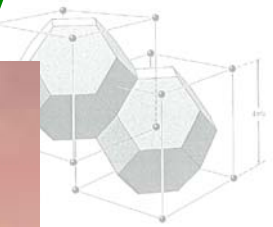
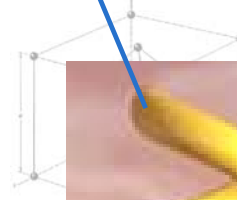
The low temperature heat capacity of pure dielectric crystalline solids is known (Chapter 5) to follow the Debye  $T^3$  law, precisely as expected from the excitation of long wavelength phonons. The same behavior was expected in glasses and other amorphous solids—the point was so obvious that it did not encourage experimental investigation.

**C. Kittel**

**Mössbauer effect**

**Glass dynamics**

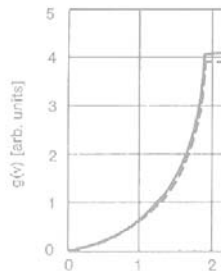
**1971:  
crash of blissful ignorance:**



**1971:  
thermodynamic anomalies !!!**

**before 1958:  
nuclear absorption increases with  $T^\circ$  ?**

**before 1971:  
glass dynamics:  
sound waves ..?**



The heat capacity of the Debye  $T^3$  law is known to be violated in glasses and other amorphous solids. The same behavior was expected in glasses and other amorphous solids. The same behavior was expected in glasses and other amorphous solids. The same behavior was expected in glasses and other amorphous solids.

specific heat:  
additional  
vibrational states?

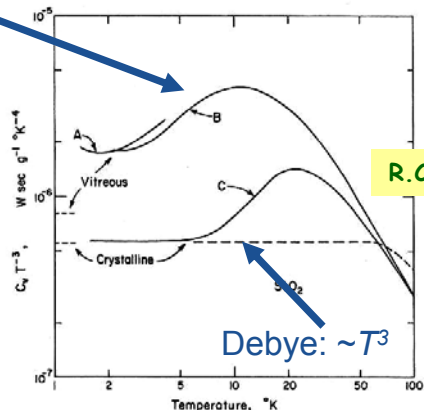


FIG. 4. Specific heat of vitreous  $\text{SiO}_2$  and crystal quartz, plotted as  $C_p T^{-3}$  vs  $T$ . A: I. R. Vitreosil (Ref. 29); B: vitreous silica (after Refs. 30–32); C:  $\alpha$ -quartz

R.C.Zeller *et al.*, PRB 4,2029,1971

thermal conductivity:  
additional source  
of scattering ?

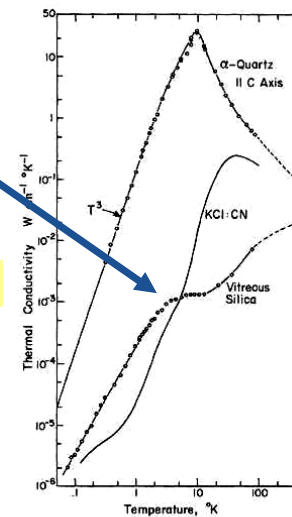
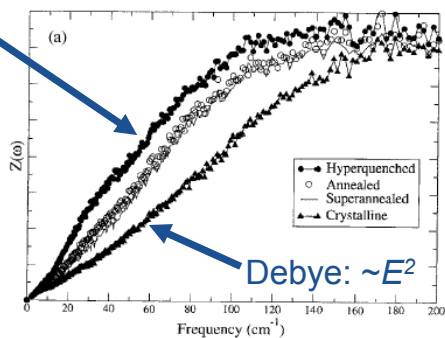


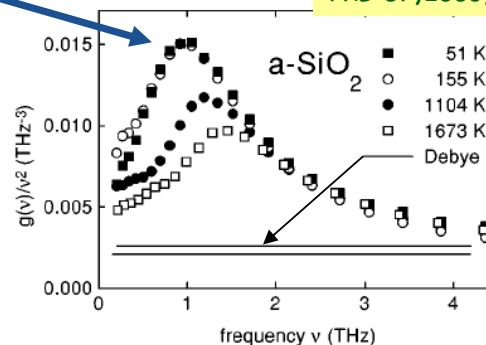
FIG. 1. Thermal conductivity of crystalline and of vitreous  $\text{SiO}_2$  and of crystalline  $\text{KCl:CN}$  ( $n_{\text{CN}} = 4.9 \times 10^{18}$ )

DOS  $g(E)$ :  
additional  
vibrational  
states !



C.A.Angel *et al.*,  
J.Phys.:Cond.Matt. 15,S1051,2003

Reduced DOS  $g(E)/E^2$ :  
the boson peak !



A.Wischnewski *et al.*,  
PRB 57,2663,1998



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boson peak glass

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Author Keywords: **Boson peak**; **Glass**; Inelastic neutron scattering. Article Outline. •  
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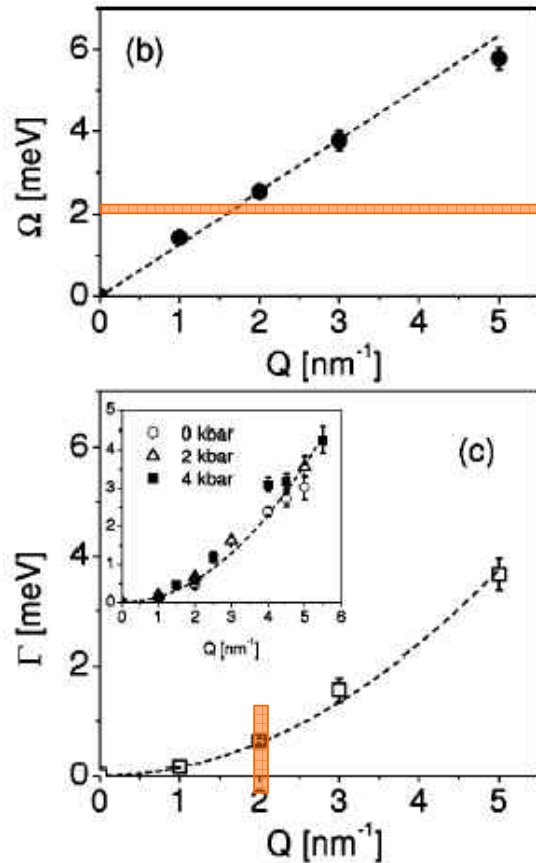
Origin of the **boson peak** in a network **glass** B2O3. Authors: , Engberg, D.; Wischniewski, A.; Buchenau, U.; Böttger, J.; Dianoux, A. J.; Sokolov, A. P.





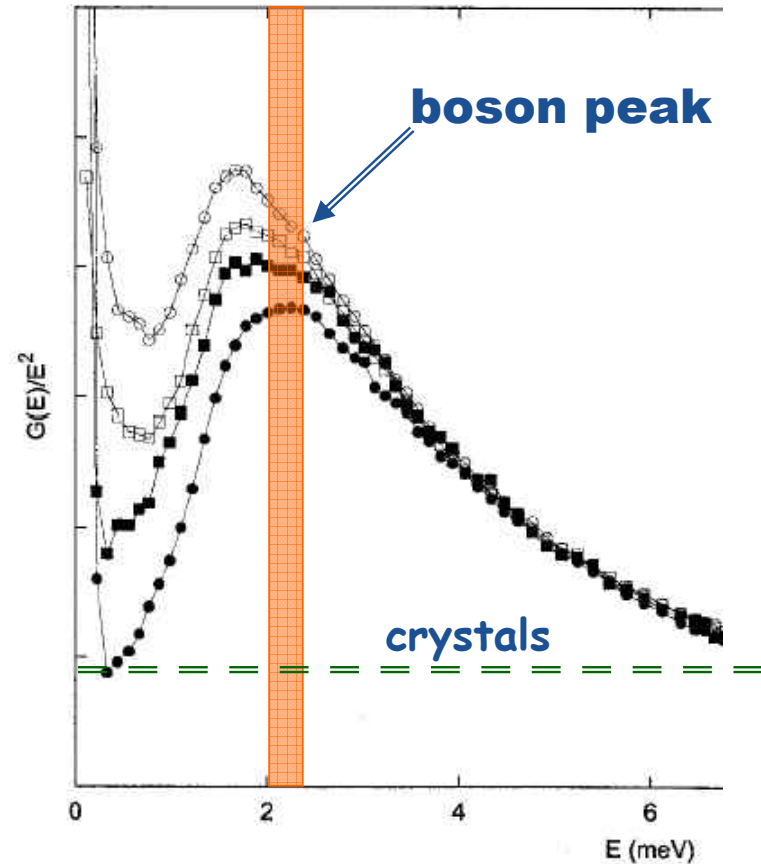


## dispersion relations



A.Mermet *et al.*, PRE 66, 31510 (2002)

## density of states



L.Savio *et al.*, Phil.Mag.B 82, 533 (2002)

Kernresonanzfluoreszenz von  $\gamma$ -Strahlung in  $\text{Ir}^{191}$

erhebt sich darüber bei Temperaturen  $T < \Theta$  eine mit abnehmender Temperatur stark ansteigende Breite der Resonanzbedingung wird also nur ein kleinerer Teil der Quanten erfüllt größer werdenden Bruchteil der Quanten erfüllt

**Mössbauer effect**

**Glass dynamics**

**1994: discovery of nuclear inelastic scattering**

**1984: excitation of nuclei by synchrotron radiation**

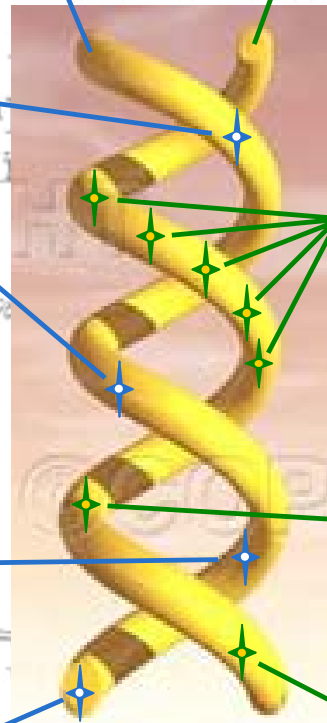
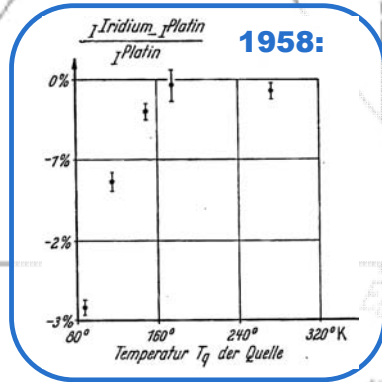
**204 001 versions of the nature of the boson peak**

**1971: thermodynamic anomalies !!!**

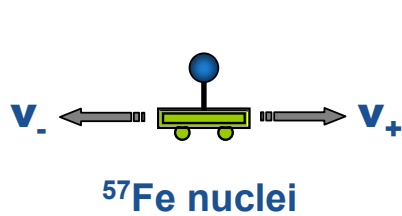
**before 1958: nuclear absorption increases with  $T^\circ$  ?**

**before 1971: glass dynamics: sound waves ..?**

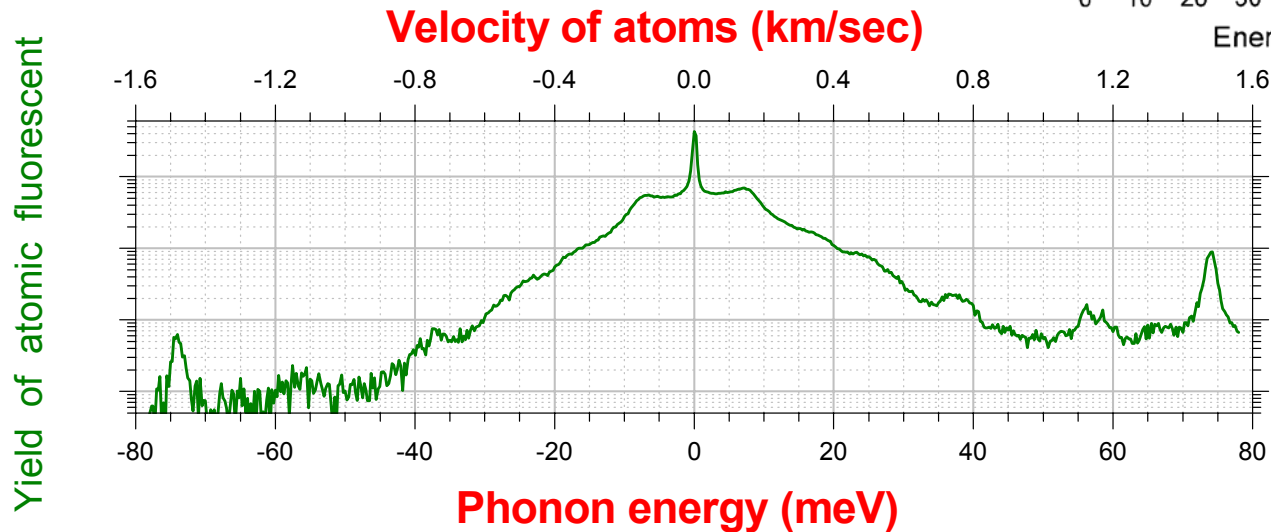
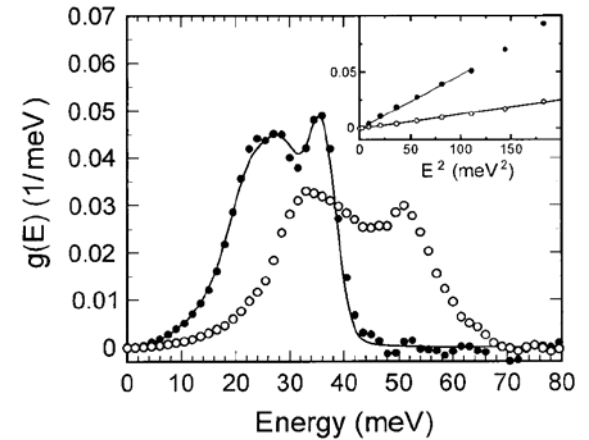
**Fortunately ...**



## Nuclear Inelastic Scattering: resonant absorption of x rays by moving nuclei:



## DOS in absolute and correct scale:



## Raman and neutron scattering



you can do almost everything,  
but not always convenient  
and not necessarily precise

## Nuclear inelastic scattering



you can only cut,  
but precisely, sharp, deep,  
and exactly where you need it



## 4. Versuchsanordnung

Fig. 2 zeigt die Versuchsanordnung, Fig. 3 den Kryostaten. Die Absorber, zwei je etwa 0,4 mm d bzw. Platinbleche von 35 mm Durchmesser waren der Abkühlung eine ungehinderte Kontraktion d

Untersucht wurde die Absorption der beim ausgesandten 129 keV Gammastrahlung in Iridium Zerfallschema [7] und das beobachtete Spektrum,

der 95d-Aktivität von  $\text{Os}^{185}$  enthält [8]. Die härtesten beim K-Einfall von  $\text{Os}^{185}$  ausgesandten Linien von  $\text{Re}^{186}$  bei 640 keV und bei 875 keV durchsetzten die Absorber



**(i) cooling rate**

**and**  
**(ii) density**

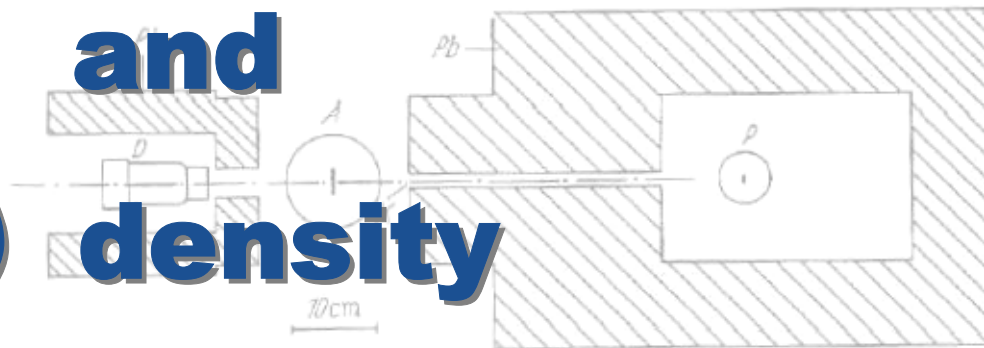
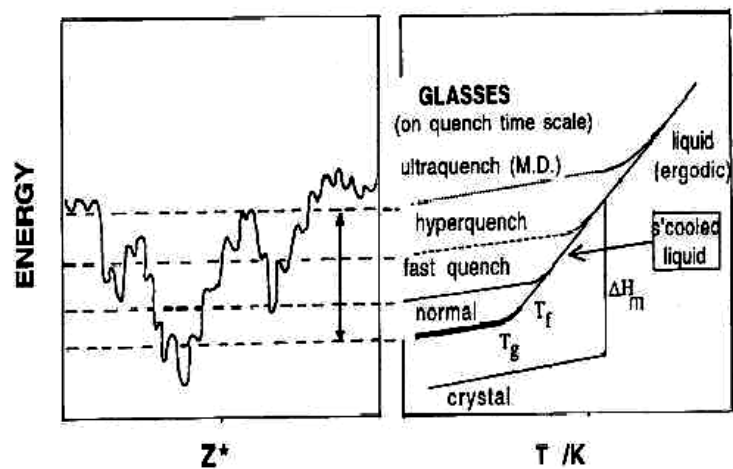
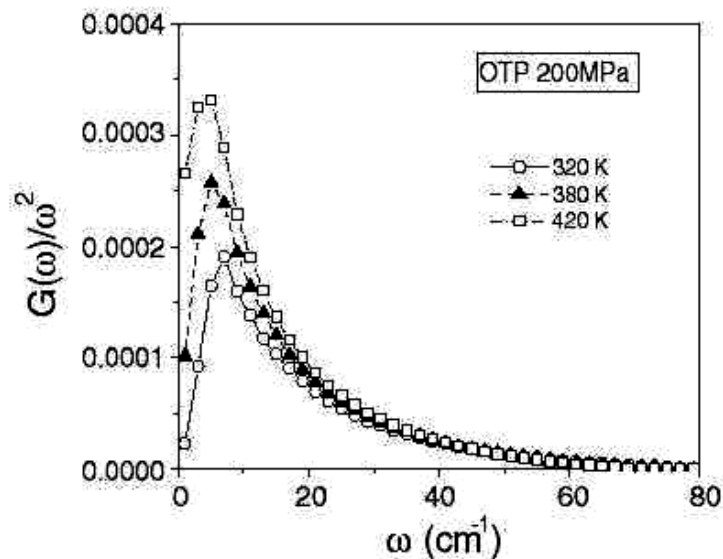


Fig. 2. Versuchsgeometrie. *A* Absorber-Kryostat; *P* Kryostat mit Quelle; *D* Detektor:  $\text{NaJ(Tl)}$ -Kristall (22 mm hoch, 40 mm Durchmesser) und Photomultiplier; *K* Kollimator (Bohrung 18 mm); *A* und *P* werden von den Armen eines schweren Stativs getragen

## cooling rate: Energy Landscape Model



**FIGURE 1.** Depiction of the relation between the energy of glasses and the rate of quenching. LHS shows the trapped system energy in relation to its energy landscape, represented in the common (but highly over-simplified) two dimensional form appropriate to constant volume systems.



**Figure 4.** The second moment of the VDOS for a model molecule inherent structures characterized by the structural temperatures peak intensity increases with increasing structural temperature.

C.A. Angell *et al.*, ~JPCM 15, S1051 (2003)

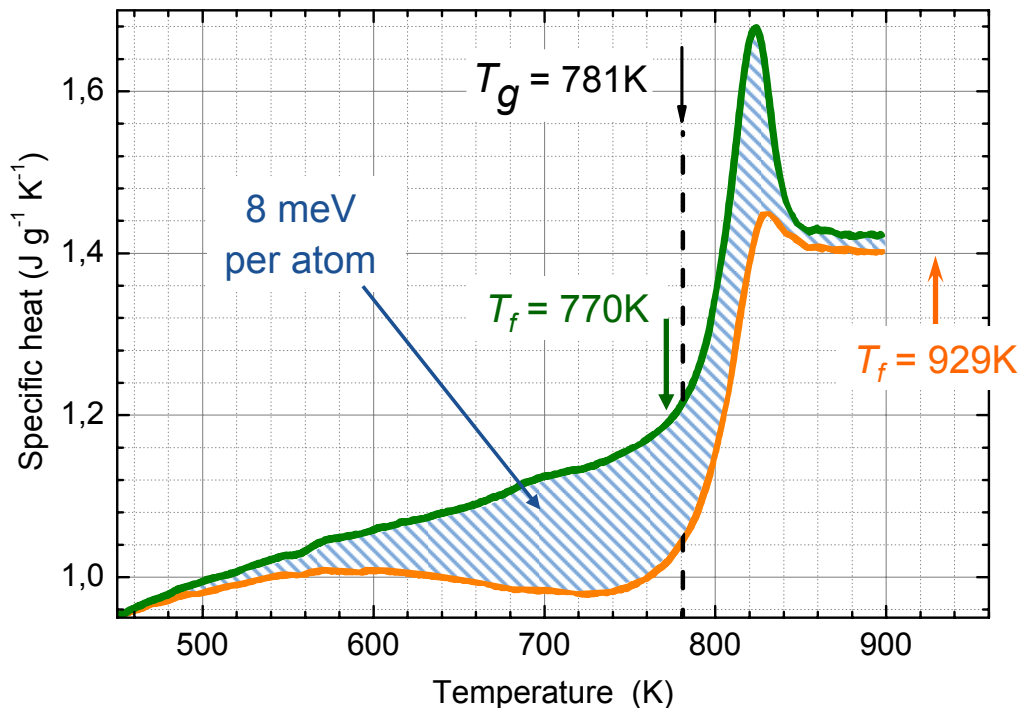
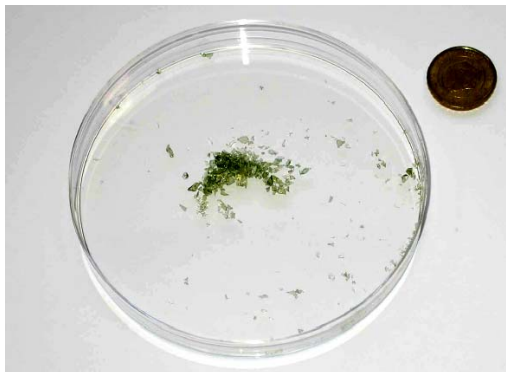
## Dependence of DOS on cooling rate:

- quenched from melt to water with a cooling rate of 1500 K/s,
- annealed for 30 min at  $T_g + 4K$ , cooled down with a rate of 2 K/s

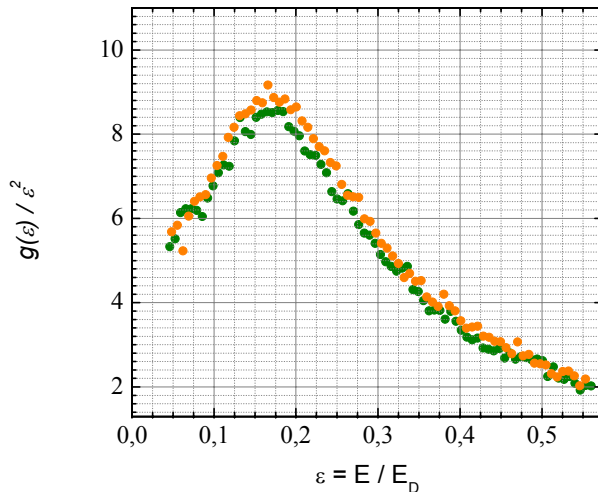
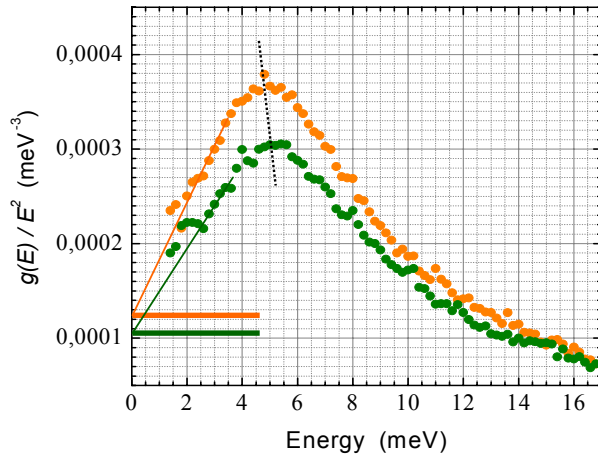
Sodium silicate glass:

$(SiO_2)_{74} (Na_2O)_{16} (FeO)_6 (CaO)_4$

$T_g = 781 K$

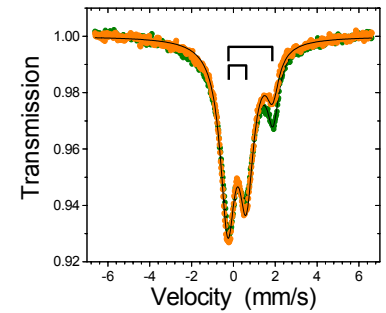


A.Monaco *et al*, PRL **96** 205502 (2006)



## microscopic properties: Mössbauer spectroscopy

- quenched
- annealed

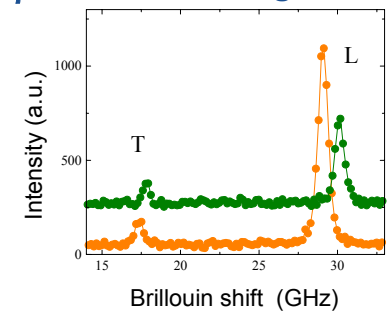


## intermediate-range properties: X-Ray Scattering



## macroscopic properties: $\rho$ & Brillouin Light Scatt.

$\rho = 2.404(1) \text{ g/cc}$   
 $\rho = 2.439(5) \text{ g/cc}$





## density: cluster model

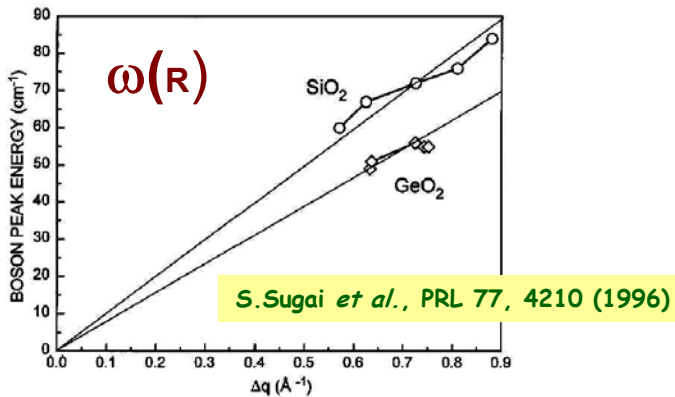
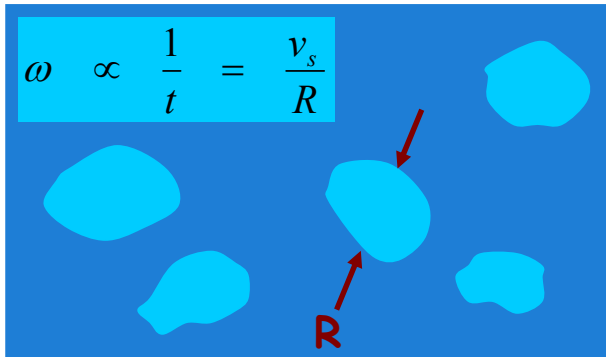
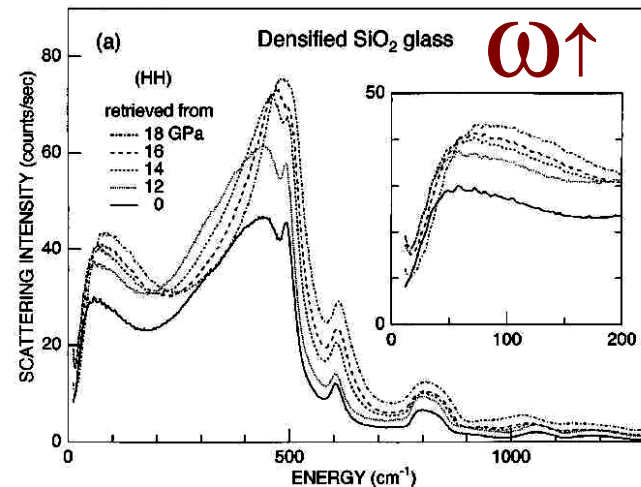
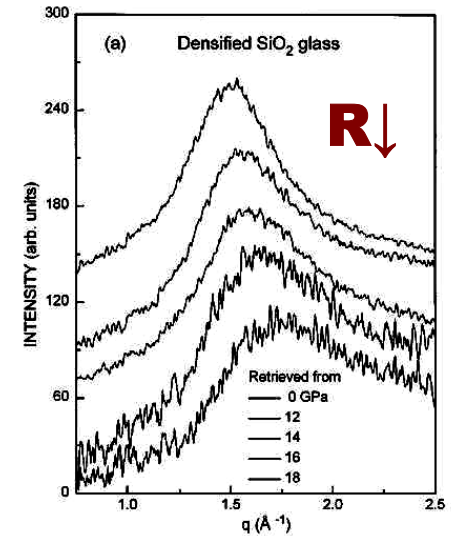


FIG. 5. Boson peak energy as a function of  $\Delta q$ .



## Dependence of DOS in glasses on density:

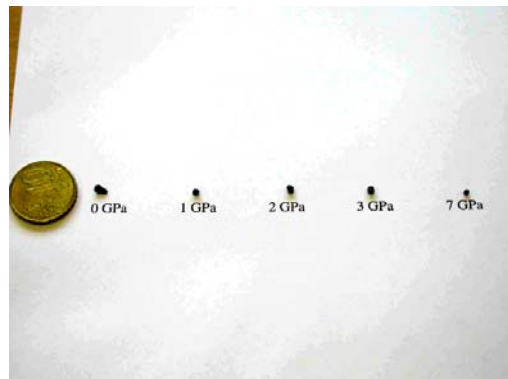
Heated up to  $T_g - 70\text{K}$ , densified for 10 min

- at 1 GPa
- at 2 GPa
- at 3 GPa

Permanently densified samples:  
sodium silicate glass

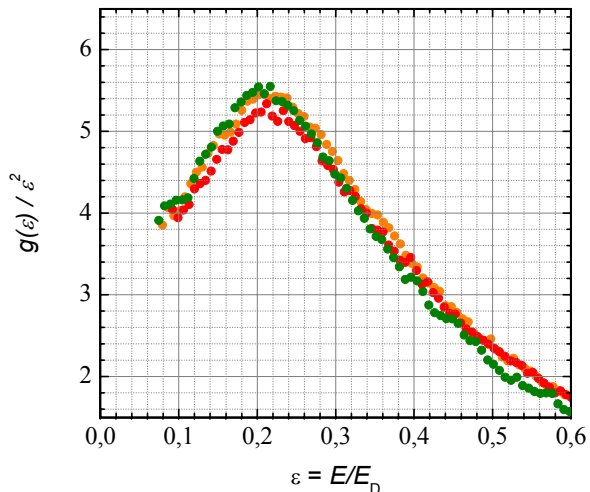
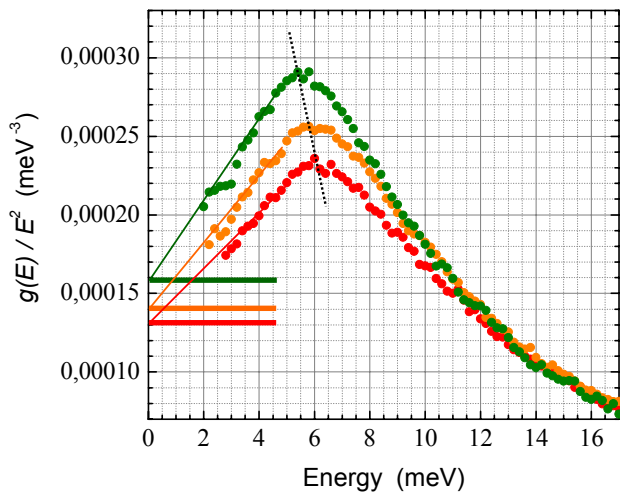


$T_g = 744 \text{ K}$



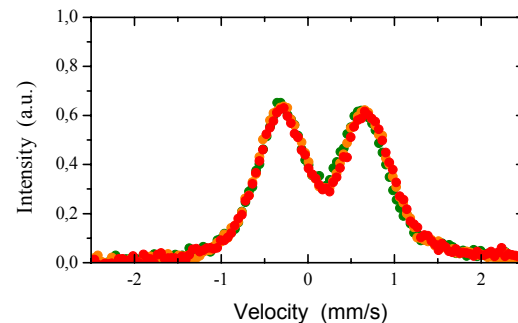
A. Monaco *et al*, PRL 97 135501 (2006)



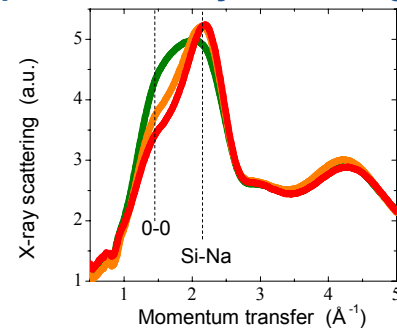


## microscopic properties: Mössbauer spectroscopy

- at 1 GPa
- at 2 GPa
- at 3 GPa

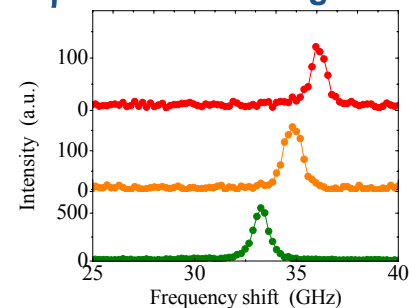


## intermediate-range properties: X-Ray Scattering



## macroscopic properties: $\rho$ & Brillouin Light Scatt.

- $\rho = 2.72(2)$  g/cc
- $\rho = 2.87(2)$  g/cc
- $\rho = 2.88(4)$  g/cc



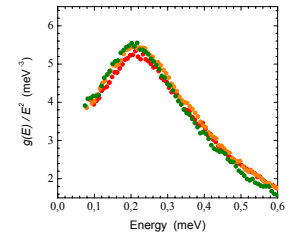
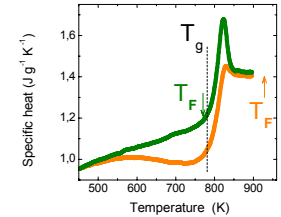
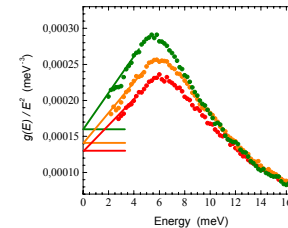
For glasses with various

cooling rate (  $T_f = T_g - 10K, T_g + 150K$  ) ;

density (  $\Delta\rho/\rho = 6\%$  ) .

Extrapolation of DOS to  $E \rightarrow 0$  is consistent with the Debye level  
 as  $E=0$  there is nothing but sound

Transformation of DOS is described by changes of elastic medium  
 as it should be for sound waves



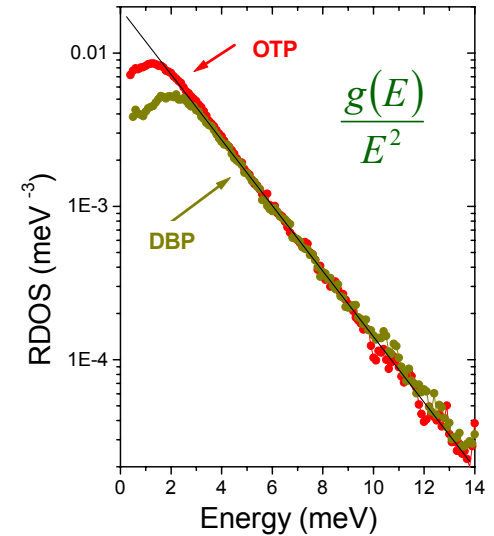
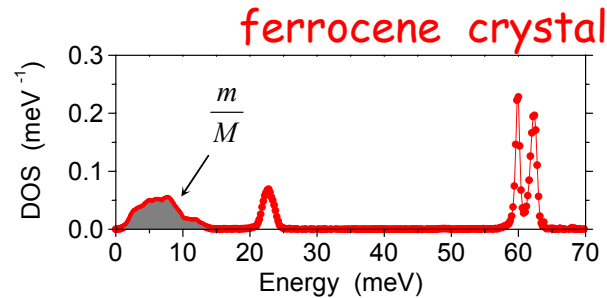
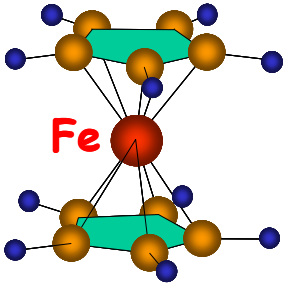
## Functional dependence?



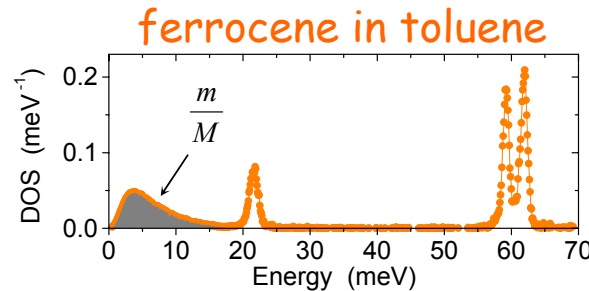
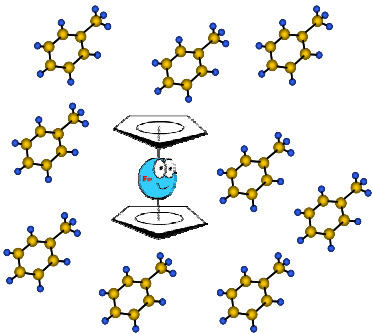
## functional dependence:

generic motions of molecules and occasional molecular modes

ferrocene



toluene

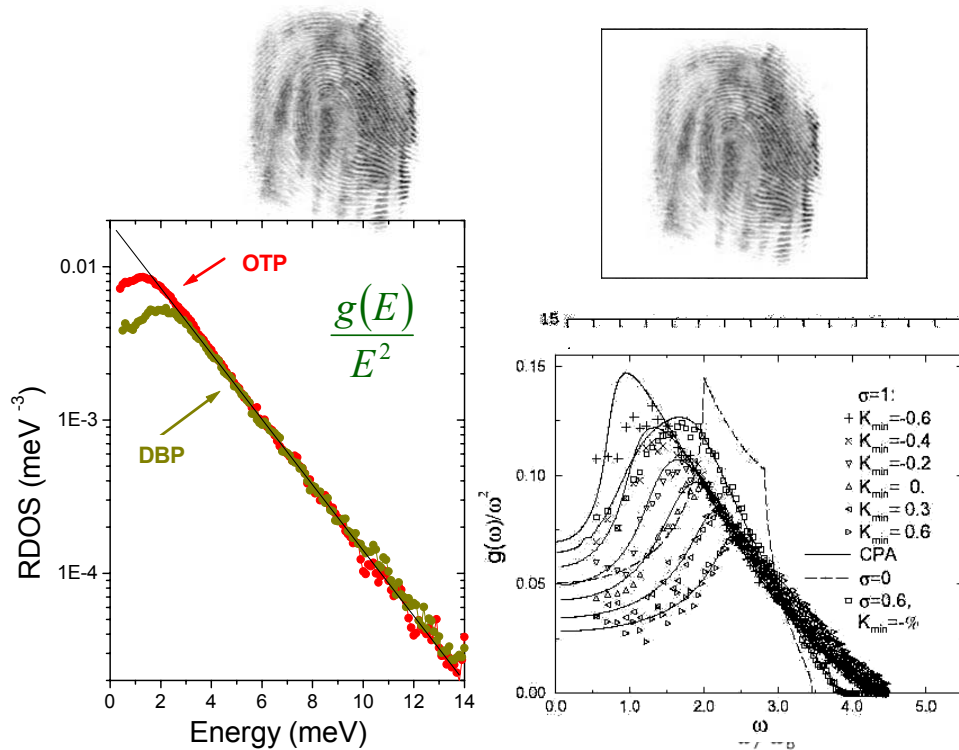


$$g(E) \propto E^2 \exp(-E/E_0)$$

$$E > E_B$$



A.Chumakov *et al*, PRL **92**, 245508 (2004)



Suspected model:	yes	no
Localized vibrations in a cluster		✓
Same, but with various cluster sizes		✓
Soft potential modes		✓
Mode coupling theory		✓
Sound waves in disordered medium	✓	

**positive match!**

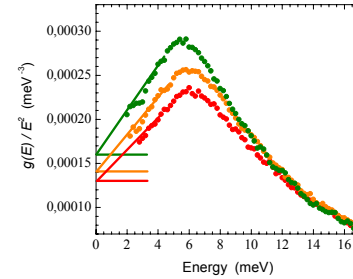
$g(E) \propto E^2 \exp(-E/E_0)$

$g(\omega) \propto \omega^2 \exp(-\omega/\omega_0)$

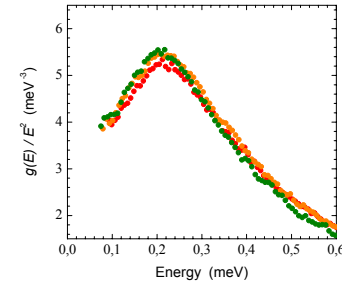
**functional behavior is consistent with sound wave model**

## Summary:

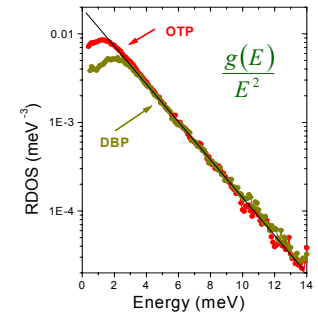
Extrapolation of DOS to  $E \rightarrow 0$  is consistent with the Debye level  
**at  $E \rightarrow 0$  there is nothing but sound**



Transformation of DOS is described by changes of elastic medium  
**entire DOS transforms like sound**



DOS follow functional dependence of sound waves  
**at  $E$  above the boson peak:  
 nothing but sound**



## a loop in understanding of glass dynamics:

**2008:**  
glass dynamics:  
sound waves ?!

**204 001 papers**  
on the nature  
of the boson peak

**1971:**  
thermodynamic  
anomalies !!!

**before 1971:**  
glass dynamics:  
sound waves ..?

**1984:**  
excitation of nuclei by  
synchrotron radiation

**1994:**  
discovery of nuclear  
inelastic scattering

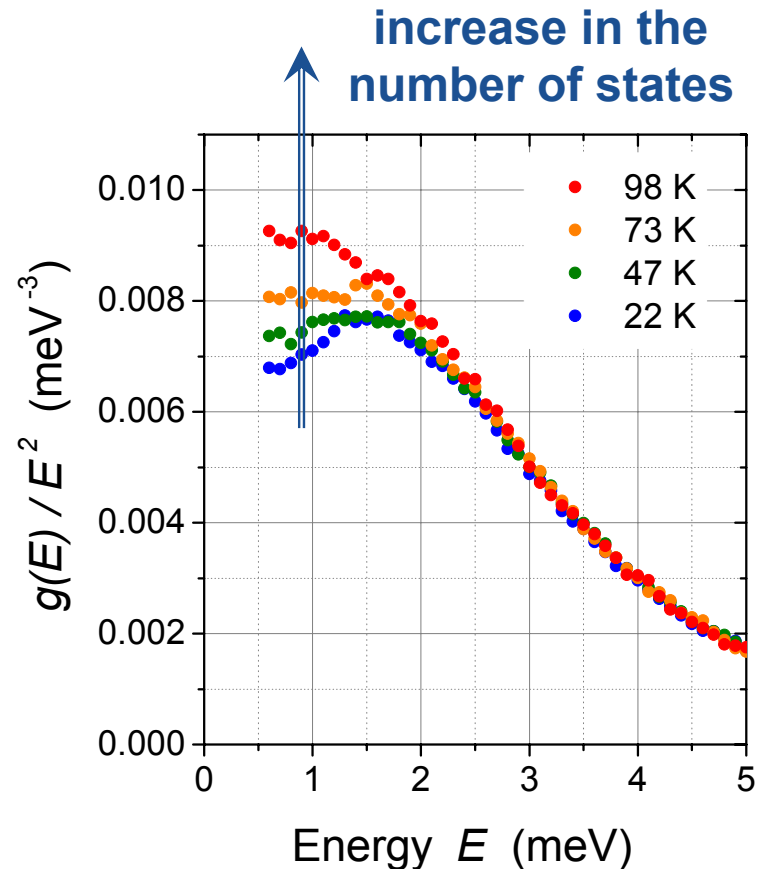
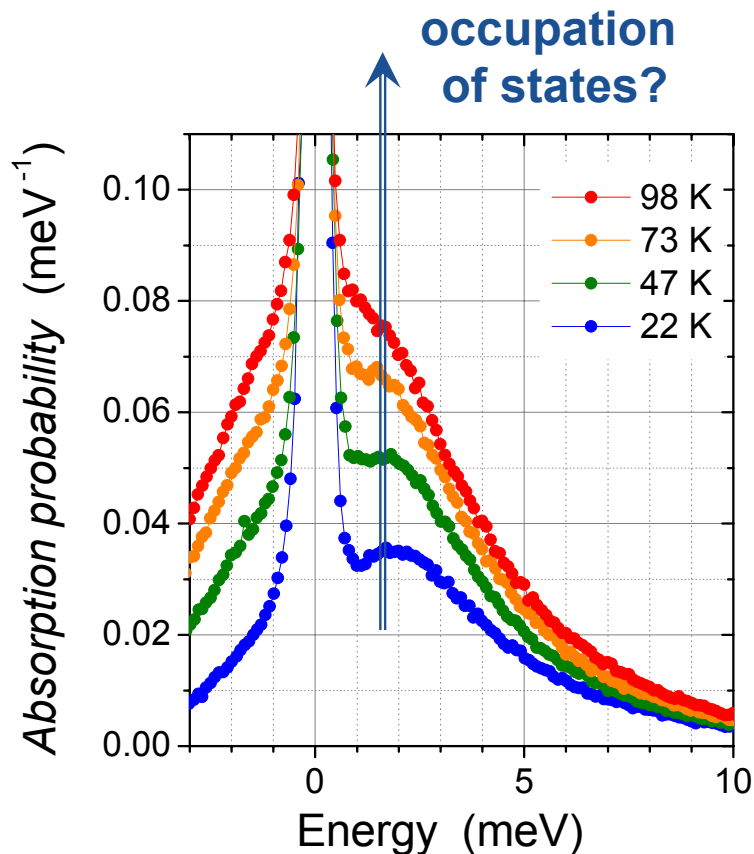
**1958:**

Temperatur $T_q$ der Quelle	Value
80°	-3%
160°	-7%
240°	-2%
320°K	0%

**before 1958:**  
nuclear absorption  
increases with  $T^\circ$  ?

Handwritten notes in the background include: "Kernresonanzfluoreszenz von Gammastrahlung in Ir<sup>191</sup>", "führen, sofern dieser nicht vollständig planparallel ist\*", "sächliche experimentelle Schwierigkeit bei der Lebenszeitmessung lag in einer sicheren Auswertung eines solchen", "Änderungen", "der Geometrie bei d", "f die Mes", "729 keV (Ir<sup>191</sup>)", "0,042 MeV", "> 5 · 10<sup>-10</sup> sec", "M1+E2 0.129 MeV", "133", "750".

## temperature dependence of nuclear absorption: toluene glass





## a loop in understanding of nuclear scattering?

